

# Fixed Income

## Basic Features of Debt Securities

### Issuer

- Sovereign governments
- Non-sovereign governments
- Supranational entities
- Quasi-government entities
- Corporations
- Special purpose entities

### Par (face) Value

- Amount borrowed by issuer
- *Premium*: Price > par value
- *Discount*: Price < par value

### Maturity

- *Money market*: Original maturity one year or less
- *Capital market*: Original maturity longer than one year
- *Tenor*: Time remaining until maturity

### Coupon

- Annual interest as a percent of par value
- Fixed or floating rate
- *Periodicity*: Coupon frequency (typically semiannual or annual)
- *Zero-coupon bond*: Issued at pure discount, pays face value at maturity

### Currency

- Denomination in which issuer will pay interest and repay principal
- *Dual-currency bond*: Pays interest in one currency and principal in another currency
- *Currency option*: Bondholder has choice of currencies in which to be paid

## Legal, Regulatory, Tax Considerations

### Indenture (Trust Deed)

- Contract between issuer and bondholders
- Administered by trustee
- Affirmative covenants: Actions issuer is required to take
- Negative covenants: Restrictions on issuer's actions

### Issuing Entities and Sources of Repayment

- Governments: Taxes or revenues from projects
- Corporations: Issuer may be parent company or subsidiary
- Special purpose entity: Bankruptcy remote from originating corporation

### National Bond Market

- *Domestic bonds*: Home currency, domestic issuer
- *Foreign bonds*: Home currency, foreign issuer

### Eurobonds

- Issued outside jurisdiction of any one country
- Denominated in currency other than that of market in which bonds are sold
- *Global bonds*: Eurobonds that also trade in a national bond market

### Taxation of Fixed-Income Securities

- Interest taxed as ordinary income
- Capital gains may be taxed at lower rate
- Original issue discount: Price increase to par is considered interest income

3

## Fixed Income Cash Flows

### Fixed-Rate Bonds

- *Bullet structure*: Periodic interest payments, all principal repaid at maturity
- *Fully amortizing*: Equal periodic payments include interest and principal
- *Partially amortizing*: Periodic payments include interest and principal, remaining principal repaid at maturity
- *Sinking fund*: Part of bond issue is redeemed periodically

### Floating-Rate Bonds

- Coupon rate increases and decreases with market interest rates
- Coupon = reference rate  $\pm$  margin
- Reference rate typically LIBOR, must match frequency of rate resets
- May have *cap* and/or *floor*
- *Variable rate note*: Margin is not fixed
- *Inverse floater*: Coupon rate changes in opposite direction to market interest rates

### Other Coupon Structures

- *Index-linked*: Coupon or principal adjusted based on published index
- *Step-up coupon*: Coupon rate increases on a schedule (bonds are typically callable)
- *Deferred coupon*: Payments do not begin immediately after issuance

### Inflation-Linked Bonds (Linkers)

- *Interest-indexed*: Coupon rate adjusted for inflation, principal remains fixed
- *Capital indexed*: Principal adjusted for inflation, coupon rate remains fixed (e.g., TIPS in U.S.)

4

## Contingency Provisions

### Callable Bonds

- Issuer may repay principal early at call price, typically par or a premium
- Call dates specified in indenture
- *Call protection*: Period after issuance during which bonds are not callable
- Higher yield compared to same bond without embedded call, unless bond has a *make-whole provision*

### Puttable Bonds

- Bondholder may sell bond back to issuer at put price, typically par
- Lower yield compared to same bond without embedded put

### Convertible Bonds

- Bondholder may exchange bond for specified number of shares of common stock
- Lower yield compared to same bond without conversion feature
- *Contingent convertible (CoCo)*: Converts automatically if specified event occurs

### Styles of Embedded Options

- *American*: Callable any time after first call date
- *European*: Callable only on call date
- *Bermuda*: Callable on specified dates after first call date

### Warrants

- Bondholder may purchase common shares at specified exercise price, but retains bond
- Lower yield compared to same bond without warrants

5

## Primary and Secondary Markets

### Primary Market

- *Public offerings*: underwritten, best efforts, auctions
- *Private placements*
- *Grey market*: Bonds traded on when-issued basis

### Corporate Debt

- *Bank loans*: Bilateral (one bank), syndicated (multiple banks)
- *Commercial paper*: Maturity < 270 days in U.S.; maturity < 365 days for Eurocommercial paper
- *Bonds*: Term maturity structure or serial bond issue
- *Medium-term notes*: Buyer specifies desired maturity

### Structured Financial Instruments

- Change risk profile of debt securities (often by combining debt security with a derivative security)
- Asset-backed securities, collateralized debt obligations
  - Yield enhancement—credit-linked notes
  - Capital protected instruments, participation instruments, leveraged instruments

### Secondary Market

- Previously issued bonds
- Most bonds trade in dealer/OTC market; some are exchange-traded
- Settlement: T+2 or T+3 for corporate bonds; T+1 or same day for government bonds; same-day for money market securities

### Repurchase Agreements

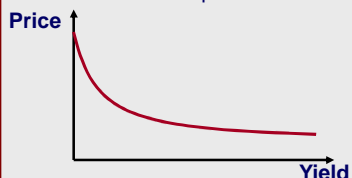
- Source of borrowing for dealers
- Sell bond to counterparty, agree to buy back at higher price
- Repo rate = implied interest rate
- Repo margin (haircut): Percent difference between loan amount and bond value

6

## Fixed Income Valuation

### Price-Yield Relationship

- Price = PV of future cash flows, discounted at YTM
- YTM ↑, price ↓
- YTM ↓, price ↑
- Convex relationship



### Matrix Pricing

- Bonds with same credit quality
- Average YTM for each maturity
- Adjust for maturity differences with linear interpolation

### Relationships Among Bond Features

- If coupon rate > YTM, price > par value
  - If coupon rate < YTM, price < par value
- Other things equal:
- Lower coupon rate increases duration; zero-coupon bonds have greatest duration
  - Longer maturity increases duration
- Capital gains/losses are measured relative to *constant-yield price trajectory*

### Price Quotations

- Full (invoice, dirty) price for semiannual = price at last coupon  $\times (1 + \text{YTM}/2)^{\text{days}/182}$
- Full price – Accrued interest = Flat price
- Accrued interest = coupon times portion of coupon period since last coupon (e.g., days/182)
- 30/360 for corporate, actual/actual for government

7

## Spot and Forward Rates

### Spot and Forward Rates

- *Spot rate*: Discount rate for single payment in the future
- *Forward rate*: Rate today for a loan to be made in the future

### Spot Rates From Forward Rates

Example:

$$s_1 = 3\%, 1y1y = 5\%, 2y1y = 6\%$$

$$(1 + s_3)^3 = (1 + s_1) \times (1 + 1y1y) \times (1 + 2y1y)$$

$$s_3 = (1.03 \times 1.05 \times 1.06)^{1/3} - 1 = 4.66\%$$

Can value bond using forward or spot rates

### Forward Rates From Spot Rates

Example: To calculate 2y1y:

$$(1 + s_3)^3 = (1 + s_2)^2 \times (1 + 2y1y)$$

$$2y1y = 1.14639 / 1.0815 - 1 = 1.06 = 6\%$$

### Yield Curve (Term Structure)

- Shows similar rates over various maturities
- Spot yield curve (strip curve, zero curve)
- Coupon yield curve
- Par bond yield curve: Derived from spot yield curve

8

## Yield Measures

### Fixed Coupon Bonds

- *Yield-to-maturity (YTM)* assumes bond held to maturity, no default, cash flows can be reinvested at YTM, flat yield curve
- *Effective yield* is compound rate of return
- *Semiannual-bond basis YTM* =  $2 \times$  semiannual discount rate
- *Street convention* uses stated coupon dates; *true yield* uses actual coupon dates
- *Current yield* = annual cash flows / bond price
- *Simple yield* adjusts current yield for amortization of premium or discount
- *Yield to call (YTC)* may be calculated to each call date and price; lowest of YTCs or YTM is *yield-to-worst*
- *Option-adjusted yield* removes effect of embedded option from YTM

### Floating-Rate Notes

- *Quoted margin* is number of basis points added to reference rate
- *Required margin* or *discount margin* is number of basis points required to return price to par at reset date
- If quoted margin < required margin, FRN will be priced at discount
- If quoted margin > required margin, FRN will be priced at premium
- Change in credit quality can cause required margin to be different from quoted margin

### Money Market Yields

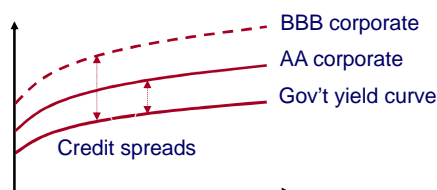
- Discount basis or add-on yields
- 360-day or 365-day years
- *Bond-equivalent yield* is add-on yield using 365-day year

9

## Yield Spreads

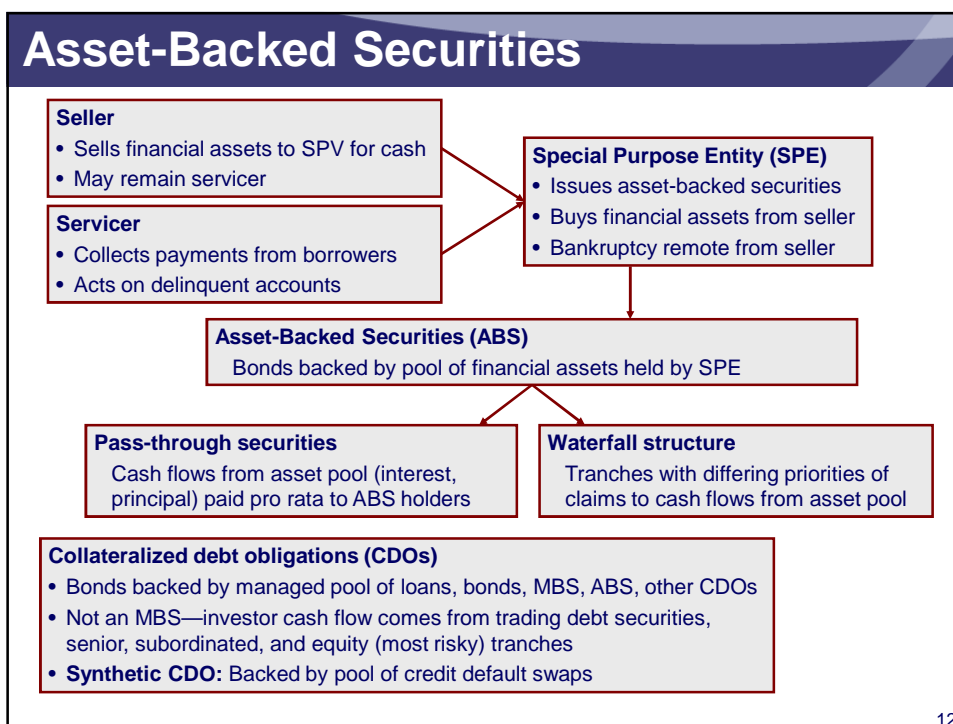
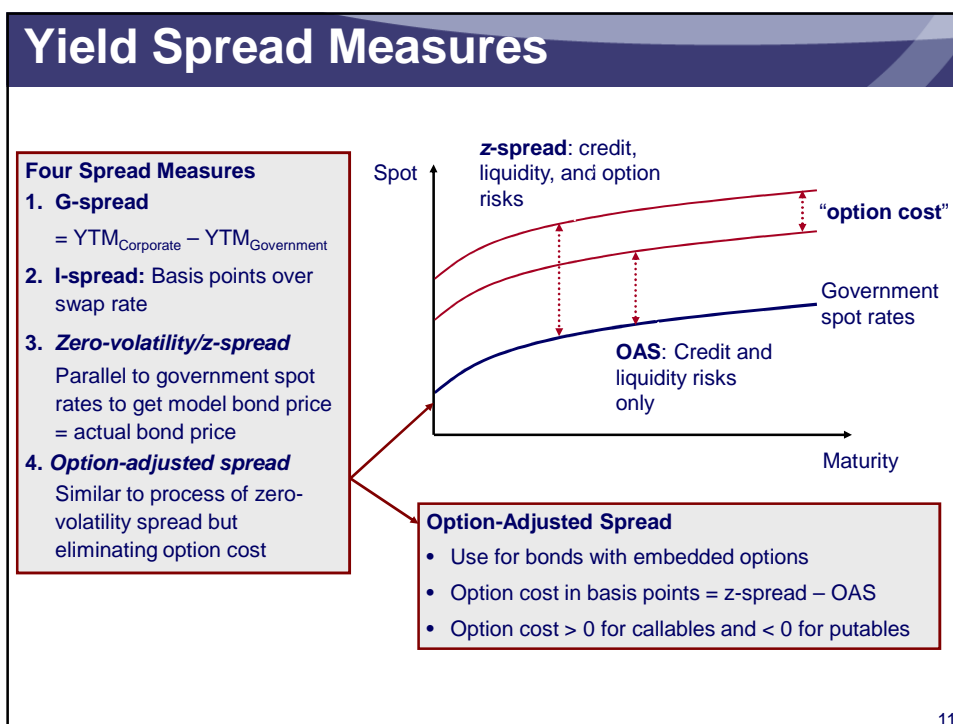
### Spread Considerations

- Credit spread: Depends on credit rating and economic conditions
- Embedded **call** option will widen spread
- Embedded **put** or **conversion** option will narrow spread
- Greater liquidity or larger issue narrows spread



**Risk Premium:** Taxation  
Liquidity  
Credit Risk

10



## Asset-Backed Securities

### Agency Residential MBS

- **GNMA:** Government agency; MBS backed by full faith and credit of U.S. government
- **FNMA, FHLMC:** Government-sponsored enterprises; no explicit guarantee by U.S. government
- Pools may only include conforming loans (e.g., maximum loan-to-value ratio, minimum documentation)
- Issue pass-through securities

### Non-agency Residential MBS

- May include non-conforming loans
- **External credit enhancement:** Third-party guarantee
- **Internal credit enhancement:** Cash reserve funds, excess spread, overcollateralization, senior/subordinated structure

### Prepayment Risks

- **Contraction risk:** Faster-than-expected prepayments (typically due to decreasing interest rates) result in earlier return of principal
- **Extension risk:** Slower-than-expected prepayments (typically due to increasing interest rates) result in later return of principal

### Collateralized Mortgage Obligations (CMOs)

- Bonds backed by pools of MBS
- Tranches with differing exposure to contraction and extension risk
- **Sequential pay CMO:** Principal payments flow to each tranche in sequence until it is paid off
- **Planned amortization class (PAC) CMO:** Scheduled principal payments to PAC classes; contraction and extension risks absorbed by support tranches if prepayment rate remains within initial PAC collar

13

## Asset-Backed Securities

### Analyzing Mortgage-Backed Securities

- **Weighted average maturity (WAM)** and **weighted average coupon (WAC)** of all mortgages in pool
- **Weighted average life** < WAM due to prepayments
- Estimated prepayment rate stated relative to **PSA benchmark** (e.g., 150 PSA)
- **Single monthly mortality rate (SMM):** Percentage by which prepayments reduce month-end principal
- **Conditional prepayment rate (CPR):** Annualized measure of prepayments

### Commercial MBS

- Backed by mortgages on commercial real estate
- Structured with tranches
- Non-recourse loans; must analyze credit risk of properties instead of borrowers
- **Loan-level call protection:** Prepayment lockout, penalty points, defeasance, yield maintenance charges

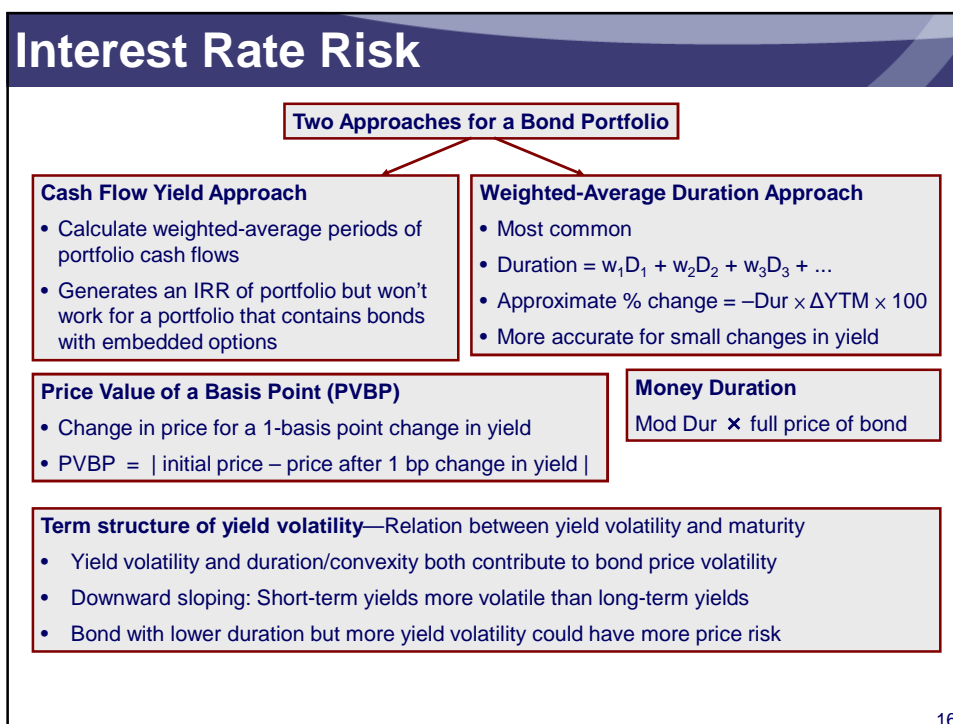
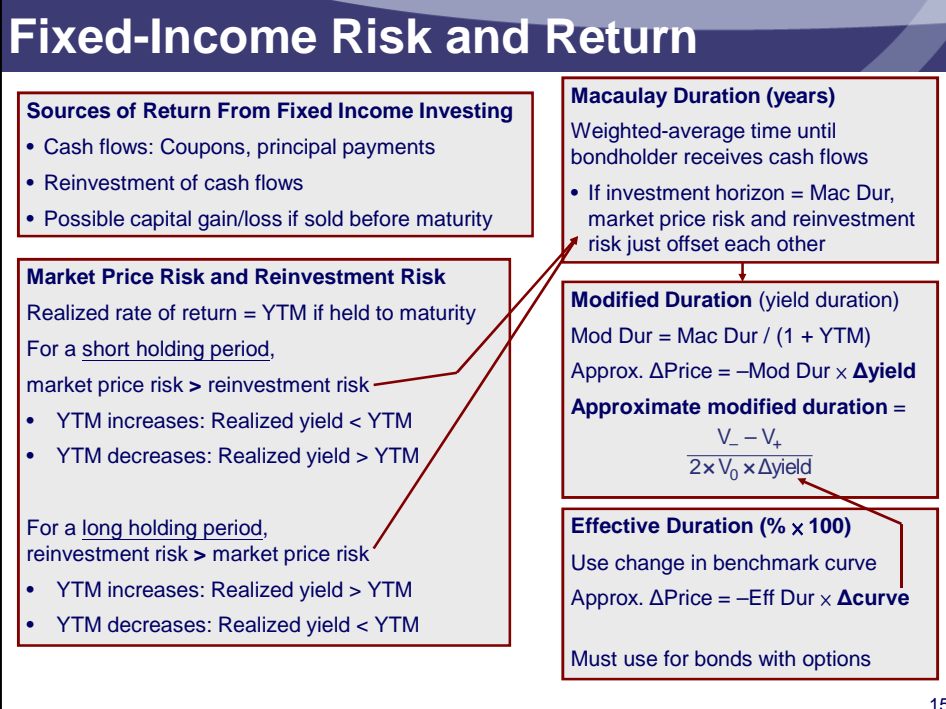
### Auto loan ABS

- Typically 3 to 5 year auto loans
- Prepayments typically result from trade-ins, insurance claims
- ABS include credit enhancement

### Credit card ABS

- Pool of revolving debt
- **Lockout period:** Interest paid to ABS holders, principal payments used to buy more credit card debt

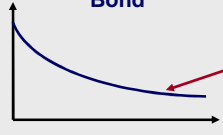
14





## Interest Rate Risk

**Option-Free Bond**

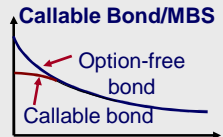


Note the slope is getting flatter from left to right: This is **positive convexity**

**Interest rate risk = price volatility**

- Prices rise at increasing rate as yields fall
- Prices fall at decreasing rate as yields rise

**Callable Bond/MBS**

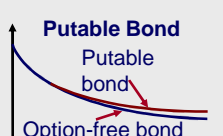


Option-free bond  
Callable bond

Moving from left to right, note **negative convexity** at low yields (but positive convexity at higher yields)

- Price compression: As yields **fall**, prices **rise** at a decreasing rate

**Puttable Bond**



Puttable bond  
Option-free bond

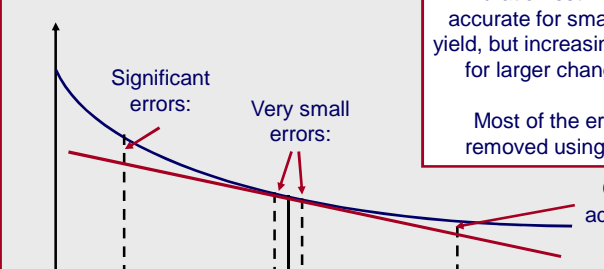
As for an option-free bond, curve exhibits **positive convexity** at all yields

- Price compression: As yields **rise**, prices **fall** at a decreasing rate

17

## Interest Rate Risk

**Convexity Improves the Picture**



Significant errors:

Very small errors:

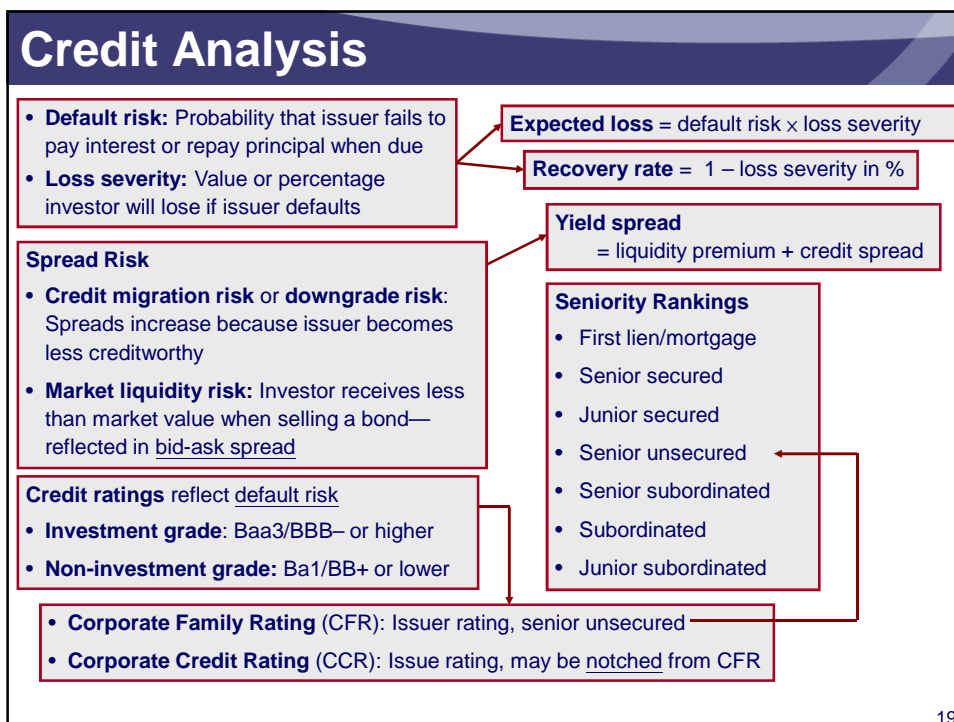
Convexity will adjust for most of this error

Duration estimate is quite accurate for small changes in yield, but increasingly inaccurate for larger changes in yield

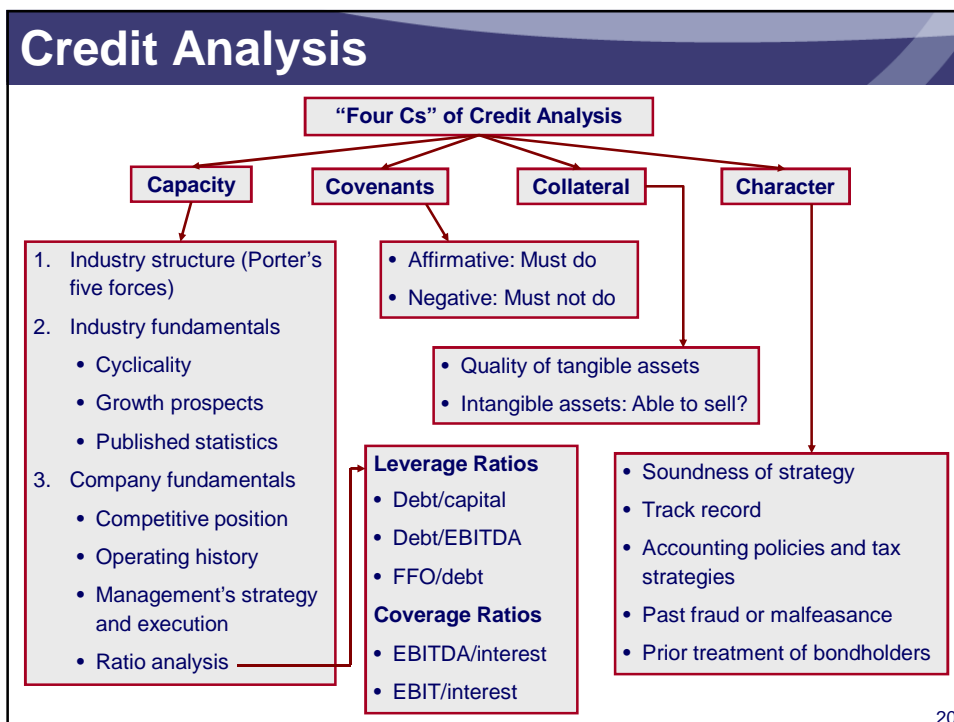
Most of the error can be removed using **convexity**

- Approximate convexity =  $[V_{+} + V_{-} - 2V_0] / [(\Delta YTM)^2 V_0]$
- Combining duration and convexity, percentage change in full bond price:  
 $\% \Delta \text{ full bond price} = -\text{annual modified duration} (\Delta YTM) + \frac{1}{2} \text{annual convexity} (\Delta YTM)^2$

18



19



20

